

# Computer Program Descriptions

## Analysis of Straight Tapered Microstrip Transmission Lines—ASTMIC

**PURPOSE:** The program ASTMIC calculates the input impedance of straight tapered microstrip transmission lines terminated with arbitrary loads.

**LANGUAGE:** FORTAN-IV; 247 cards.

**AUTHORS:** K. N. Suryanarayana Rao, V. Mahadevan, and S. P. Kosta are with the ISRO Satellite Systems Project, Peenya, Bangalore, India.

**AVAILABILITY:** ASIS-NAPS Document No. 02930.

**DESCRIPTION:** A straight tapered microstrip transmission line [1], in which the width of the taper varies uniformly over the length of the line,

is easy to fabricate and is commonly used as impedance transforming sections in microwave circuit designs. A computer program for the analysis of such lines has been described here. For any fixed degree of taper, the program calculates the input impedance for various frequencies and load impedances.

The program is built around the method, which treats the tapered line as a cascaded combination of a large number of uniform transmission line sections of small length (Fig. 1). This discretization allows the use of usual transmission line equations for the analysis. Starting from the load end, the input impedance of any section is treated as the load impedance of the next section. The input impedance of any section is given by

$$Z_{in,n} = Z_{0,n} \frac{Z_{L,n} + Z_{0,n} \tanh(\alpha_n + j\beta_n)l}{Z_{0,n} + Z_{L,n} \tanh(\alpha_n + j\beta_n)l}. \quad (1)$$

Also

$$Z_{in,n} = Z_{L,n-1} \quad (2)$$

and

$$Z_{in} = Z_{in,n(n=1)} \quad (3)$$

where

- $Z_{in,n}$  input impedance of the  $n$ th section;
- $Z_{0,n}$  characteristic impedance of the  $n$ th section;
- $Z_{L,n}$  load impedance of the  $n$ th section;
- $\alpha_n$  attenuation constant of the  $n$ th section;
- $\beta_n$  phase constant for the  $n$ th section;
- $l$  length of each section;
- $Z_{in}$  input impedance of the microstrip transmission line.

For each section, the characteristic impedance and the phase constant are obtained from Wheeler's expressions [2], [3]. The attenuation constant is obtained from the microstrip line losses [4].

The accuracy of the computation depends on the number of sections chosen. An accuracy criterion has been chosen such that the computer time is not unnecessarily high, while yielding acceptable accuracy. The required number of sections ( $N$ ) meets the criterion that the computed value of the magnitude of the

Manuscript received January 1976.

See NAPS document No. 02930 for 23 pages of supplementary material. Order from ASIS/NAPS c/o Microfiche Publications, P.O. Box 3513, Grand Central Station, New York, NY 10017. Remit in advance for each NAPS accession number. Institutions and organizations may use purchase orders when ordering; however, there is a billing charge for this service. Make checks payable to Microfiche Publications. Photocopies are \$5.75. Microfiche are \$3.00. Outside of the United States and Canada, postage is \$3.00 for a photocopy or \$1.50 for a fiche.

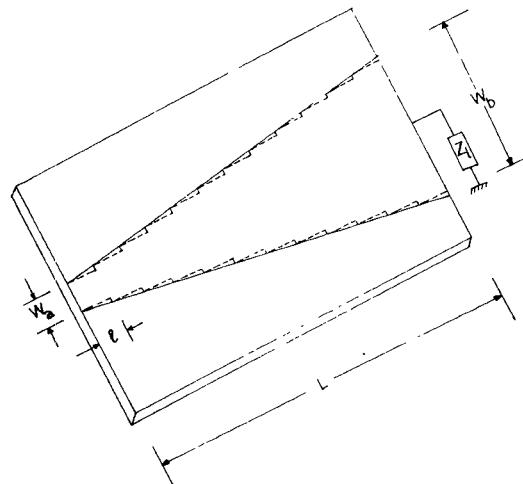


Fig. 1. Schematic diagram of the straight tapered microstrip transmission line showing the division of the tapered transmission line into a number of uniform transmission line sections.

input impedance for  $N$  sections is within 1 percent of the final asymptotic value. The value of  $N$  is found from the following empirical relation:

$$N = 70(1 + p) \quad (4)$$

where  $p$  is the percentage difference in the calculated values of  $Z_{in}$  for 35 and 45 number of sections. This relation was arrived at after many runs of program involving several cases of different degrees of taper and loads.

The value of  $N$  required for a desired accuracy is mainly a function of the degree of taper. Normally, the value of  $N$  is less than 500, but can be more for very high degrees of taper, such as a tapered line with an end impedance ratio of 50 and an electrical length of less than a wavelength. For all practically encountered tapers, the value of  $N$  lies between 70 and 250.

The input parameters for the program are the end characteristic impedances and the physical length of the tapered line, height, and dielectric constant of the substrate, conductivity of the microstrip conductor material, frequencies, and the respective load impedances. The output parameters are  $Z_{in}$  real and imaginary, magnitude and phase.

The program does not have any constraints and takes all degrees of taper and load impedances.

## ACKNOWLEDGMENT

The authors wish to thank Prof. U. R. Rao for his encouragement. They also wish to thank the members of the Antenna and Microwave Group, ISSP, and S. S. Deshikachar for their suggestions and programming assistance.

## REFERENCES

- [1] K. N. Suryanarayana Rao and S. P. Kosta, "On tapered microstrip transmission lines," *J. Asia Electronics Union*, vol. VII, pp. 34-36, 1974.
- [2] H. A. Wheeler, "Transmission line properties of parallel coupled wide strips by conformal mapping approximation," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-12, pp. 280-289, May 1964.
- [3] H. A. Wheeler, "Transmission line properties of parallel strips separated by a dielectric sheet," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-13, pp. 172-185, Mar. 1965.
- [4] M. Caulton, "Film technology in microwave integrated circuits," *Proc. IEEE*, vol. 59, pp. 1481-1489, Oct. 1971.